

A Brief Review of Nature-Inspired Computing Based Algorithms And Their Applications

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Abstract

Real world problems are hard and computationally incentive. Nature based solutions can be a great source of inspiration for optimizing challenging problems. Researchers are putting in lot of efforts to study and mimic the nature for finding optimal or near optimal solution of a problem. Nature inspired algorithms (NIC) can be broadly classified into evolutionary or swarm based algorithms based on the source of inspiration. In this paper we will study some of nature inspired computing based algorithms like Ant Colony Optimization (ACO), Particle Swarm optimization (PSO), Honey Bee Optimization algorithm, Genetic algorithm (GA) along with their applications.

Keywords:- Nature inspired computing, Optimization, ACO, PSO, GA

1Introduction

Nature has inspired the researchers to propose algorithms for solving a wide range of complex computation and optimization problems. Learning from nature how it handles complex problems for which traditional methods do not work effectively will help in developing the intelligent system. Nature always evolves and moves towards optimization, using the same concept solution of hard real-world problems can be analyzed. Nature has many properties like self organization flexibility, robustness, collective work are used to derive nature inspired algorithms. Different nature inspired optimization algorithms are classified as swarm intelligence and evolutionary

algorithms are derived from nature and are being used by different applications. Researchers and scientists have come up with different applications of nature-inspired algorithms ranging from engineering design, business planning, water distribution etc with an aim of achieving optimization. Optimization means tuning input values for a given function so as to minimize or maximize the output [1]. The optimized solution can either be the best solution or the solution relatively close to the best solution. The objective of optimization is problem specific which can be minimizing cost, energy consumption or maximizing the profit of a business or maximizing the network bandwidth utilization. In this paper nature inspired algorithms are discussed along with their different applications in real life.

2. BRIEF REPRESENTATION OF SELECTED NATURE INSPIRED ALGORITHMS

a) Ant Colony Optimization (ACO)

ACO algorithm was proposed in early 1990's by M. Dorigo [2][3][4] which is based on the behavior of ants and a phenomenon known as stigmergy[94] (term introduced by French biologist in 1959 and means a mechanism of indirect co-ordination, through an environment, between agents and action) providing ants the ability to find the shortest path between ant's nest and food source by building path from pheromone[95] traces. Pheromone is a chemical substance laid down by the ant along their trail which decay over time. Path with most intensity of pheromones is the path which is followed by most ants. This indirect communication between ants enables them to find the optimum solution i.e. shortest path. Algorithm or pseudo code for ACO [5] is presented.

Algorithm 1

Begin

Generate Initialize population and pheromone matrix

fitness computation of initial population

While (stopping criterion not satisfied) **do**

Set position each ant as starting node

Repeat

For each ant **do**

Choose next node by applying the state transition rule

Apply step by step pheromone update

End for

Until every a solution for every node is obtained

Evaluate fitness of population

Update best solution obtained

Apply Pheromone update

End While

End

Ant system can be considered as a graph where the pheromones update for edge E_{ij} joining nodes i and j is performed [6][7] as given below:

$$E_{ij} \leftarrow (1 - p) \cdot E_{ij} + \sum_{k=1}^m \Delta E_{ij}^k$$

where p is the pheromone decay rate whose value is between $(0,1)$, Total number of ants (m) and ΔE_{ij}^k is the quality of pheromones laid by the k th ant on the edge (i,j) .

Transition probability $p(c_{ij}|s_k^p)$ of k th ant moving from node i to node j is given by:

$$p(c_{ij}|s_k^p) = \begin{cases} \frac{E_{ij}^\alpha * \eta_{ij}^\beta}{\sum_{c_{ij} \in N(s_k^p)} E_{ij}^\alpha * \eta_{ij}^\beta} & \text{if } j \in N(s_k^p), \\ 0 & \text{otherwise} \end{cases} \quad (1)$$

Where η is an optional weighting function and $\eta = \frac{1}{d_{ij}}$, d_{ij} is the length of component c_{ij} , α and β are positive numbers and control the relative importance of pheromone and heuristic information.

b) PSO

PSO algorithm was proposed in [98] and is an evolutionary computation technique based on research of the flock of birds[36] searching a food source[36]. PSO algorithm a birds group is searching for food in an area where only one piece of food is available and birds don't have the

information about the exact location of the food source. Birds know the distance of food source from current location is. In this algorithm, all birds of the flock change their velocity based on their past experience and by following the bird nearest to the food. Each bird or solution in PSO is called particle[99]. Each particle's coordinates (possible solution in the search space) is represented by two vectors position x_i and velocity v_i . N-dimensional search space[100] of each particle can be represented by $x_i=[x_{i1}, x_{i2}, x_{i3} \dots x_{iN}]$ and velocity $v_i=[v_{i1}, v_{i2}, v_{i3} \dots v_{iN}]$. Searching the optimized solution in the search space is based on the particle's best position $pbest$ and best position so far among the entire group of particles $gbest$. PSO optimization technique can be simply represented as:

$$v_i^{n+1} = v_i^n + c_1 r_1^n (pbest_i^n - x_i^n) + c_2 r_2^n (gbest_i^n - x_i^n) \quad (3)$$

$$x_i^{n+1} = x_i^n + v_i^{n+1} \quad (4)$$

Where c_1 and c_2 are positive acceleration constants and r_1 and r_2 are numbers in the range $[0,1]$ and are random, $pbest_i^n$ is the best possible position of the particle i achieved in n iterations and $gbest_i^n$ represents the most optimum position of the swarm in n iterations.

Changing the velocity of particle considering the particle's best performance and the best performance by the closest particle the optimum solution is searched.

Algorithm or pseudo code for PSO [91] is presented below

Algorithm 2

Begin

For each particle

Initialize particle randomly

end for

For $i=1$ **until** maximum iteration

Calculate every particle velocity (use equation 3)

Update every particle location (use equation 4)

For each particle **do**

calculate fitness for particle

if fitness better than the previous $pbest$ then

set fitness value as new pbest

end if

end for

Choose particle with the best pbest as gbest

End for

Return gbest

End

c) **ABC Algorithm**

ABC algorithm was presented by Karaboga in 2005 [63]. In ABC algorithm communication about the direction, distance and quantity of nectar at food source is done by waggle dance by a honey bee. Bees are grouped into three categories employed foragers, unemployed foragers and experienced foragers [63, 64]. Bees that have no information about the food source are classified as unemployed. Unemployed foragers can either start searching for food source from a scratch without any prior knowledge and are called Scout Bee or can be a Recruit bee that uses the information obtained by the waggle dance of another bee about the food source. Recruit bee after watching waggle dance of different bees decides about the most profitable food source. The recruited bee when finds the food source and starts extracting energy, it is classified and employed bee. Employed bee also shares information about the food source. Experienced bees use their prior knowledge for discovering new food source near their hives.

ABC algorithm uses exploration and exploitation for finding the best solution. After the food source is explored the bee memorizes the location and starts exploiting it. The bee loads the nectar from food source and unloads the nectar to a food store at their hive. Now the bee can abandon the food source, communicate with other bees about food source by waggle dance or keep foraging the food source himself without any recruitment.

Algorithm or pseudo code for ABC [65] is presented below

Algorithm 3

Begin

Initialize the food source positions.

Evaluate the food source

Fori=1 **until** maximum requirements meet

 Produce the new food sources

 Move the recruits to the food sources and determine the nactor

 Apply greedy selection

 Calculate the fitness and probability values

 Memorize the best food source found so far i.e.gBest

End for

Return gBest

End

d) **GA**

Genetic Algorithm (GA) is a evolutionary method which was presented by “John Holland” in early 1960s [67]. GA is based on the natural evolution of a biological species and can be applied for stochastic search or for finding optimal or near-optimal solution. GA is inspired by the process of selection of a solution from a population based on (the theory of Darwin) a fitness function (maximization or minimization). Solution space comprising of Individuals also known as chromosomes matures with every generation so as to provide a optimal or near optimal solution. Individuals as selected based on a selection method (roulette wheel, Boltzmann selection, tournament selection, rank selection, steady stare selection etc) from population for reproduction. Cross-over method is applied for produce a new chromosome by combining parts of parents. Produced chromosome retains the useful features of the parents and ignores less useful features.

In order to avoid local optimality [68] some (low probability) of the offspring are mutated. Mutation causes genetic diversity by bringing a small change in the chromosome’s element allele. Some the common mutation techniques are power mutation, uniform mutation, Gaussian mutation, shrink mutation etc. Chromosomes with the ‘best fitness’ value are retained

in the new population. This process continues until the desired optimal solution is obtained or process continues for max number of generations.

Algorithm or pseudo code for GA [92,93] is presented below

Algorithm 4

Begin

Input population, cross-over probability, mutation probability

Initialize chromosomes randomly

While desired optimal solution or max generations are not reached **do**

 update chromosomes by crossover and mutation operations

 Compute the fitness of each chromosome

 Save fitness values of chromosomes

 Select chromosomes by using selection method for next generation

EndWhile

Report chromosome with best fitness value as an optimal solution

End

e) **Other Algorithms**

Researchers are continuously working on different new nature inspired algorithms to find and optimal solution. NIC algorithms can be classified into different classes like bio-inspired, swarm intelligence (SI) based, chemistry-based/physics and others. Some of the well known algorithms are Cuckoo search optimization (CSO), Bat algorithm, Paddy Field Algorithm, flower pollination algorithm, Grey wolf optimizer (GWO), Glowworm Swarm Optimization, Firefly algorithm, Cat Swarm Optimization (CSO), Cuckoo search, Monkey search, Eagle strategy, Shuffled frog leaping algorithm, Big bang-big Crunch, Black hole, Gravitational search etc [88]. Researchers are working on these algorithms so as to increase their performance. For example “Parallel Big Bang–Big Crunch Global Optimization Algorithm” [89] was presented so as to increase the performance of Big bang-big crunch (B3C) [97]. “Modified cuckoo search algorithm” with rough sets for feature selection was proposed so as to handle high dimensionality data [90].

3. Applications of few selected nature inspired algorithms

Name of Algorithm	Representation	Operations	Applications	Control Parameters
ACO	Undirected Graph	Pheromone trail, update, evaporation, measure	Traveling Salesman Problem (TSP)[8,9],Text feature selection[10], Vehicle routing problem[11, 12], Face recognition [13], Cloud task scheduling [14], Training feed-forward neural networks [15], Structure-, based drug design [16], Protein folding problem[24],DNA sequencing[30],Data mining[17,18], Multi-purpose reservoir operation[19], Process planning[20],Graph coloring[21], Digital image processing [22, 23], Quadratic assignment[25,26,27], Supply chain management[28, 29], Multicasting ad-hoc networks [31,32,33],Project scheduling [34,35]	Total number of Ants, pheromone decay rate, iteration.
PSO	Dimensionality of vector for the position,speed,beststate and is Real-valued	Initializer, updater and evaluator.	Multimodal biomedical image registration[38], Iterated Prisoner's Dilemma[39], Classification of instances[40], Feature selection[41,42,43,44], web service selection[45], Power System Optimization problems [46,47], Edge detection in noisy images[48,49,50], Maximizing production[51], Scheduling problems[96] ,Vehicle routing problems[52], Artificial Neural Network[53,54,55],multi-objective,	Particles count, Dimension of particles, Range of particles, Learning factors:initialweight, themax number of iterations

			Combinatorial optimization problems, QoS in adhoc multicast[56,57], Color image segmentation[58] , sequential ordering problem, constrained portfolio optimization problem, Signature verification[59], Optimization in Electric Power Systems[60,61], computational finance applications[62], convergence analysis and parameter selection[37]	
ABC	D dimensional vector	Recruitment of bee, searching new food source.	Numerical function Optimization[66], Optimizing feature selection[65], Colormap Quantization[69], feed-forward neural networks[70], set covering problem[71], distribution systems[72], real-parameter optimization[73], engineering design[74], examination timetabling problems[75,76], scheduling in grid environments[77], optimal power flow[78], traveling salesman problem[79], image edge enhancement[80], load balancing[81]	The maximum number of iterations, number of food sources, employed unemployed bee count

Genetic Algorithm	Binary or real numbers	Selection Crossover Mutation	protein folding simulations[82,83],clustering and image segmentation[84],Data mining[85] graph and shape matching[86],genetic algorithms were used for registration of depth images, 2D shape recognition,rigid registration of 3-D curves and surfaces[87],	Population, generations, crossover and mutation probabilities, Chromosome length, chromosome encoding, and decoding	Max and
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Conclusion

This paper provides an overview of different nature inspired algorithms. Some of the well known algorithms like ACO, PSO, ABC and GA are discussed in detail along with their representation, operations and applications. Other well known algorithms are also mentioned. NIC algorithms can be used for optimizing a solution of a complex and challenging problems. The scope of this field is very vast and there is lot of areas yet to be explored.

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